

- 1 The centre  $O$  of a circle has coordinates  $(4, 7)$

The point  $A$ , on the circle, has coordinates  $(6, 11)$  and  $AOP$  is a diameter of the circle.

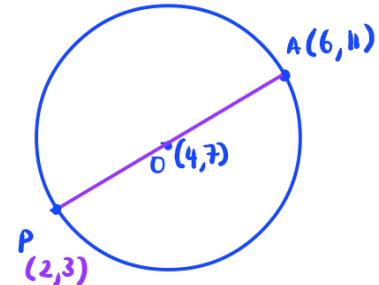
Find an equation of the tangent to the circle at the point  $P$

Finding coordinates of  $P$  :

$$\begin{aligned} x\text{-coordinate} : \frac{6+x}{2} &= 4 \\ x &= 2 \end{aligned}$$

$$\begin{aligned} y\text{-coordinate} : \frac{11+y}{2} &= 7 \\ y &= 3 \end{aligned}$$

$$P = (2, 3) \quad \textcircled{1}$$



$O$  is the midpoint of  $PA$

Finding gradient of  $AOP$  :

$$m = \frac{11-3}{6-2} = \frac{8}{4} = 2 \quad \textcircled{1}$$

Finding gradient of tangent to  $AOP$  :

$$m = -\frac{1}{2} = -\frac{1}{2} \quad \textcircled{1}$$

Equation of tangent at  $P$  :

$$3 = -\frac{1}{2}(2) + c$$

$$c = 4$$

$$y = -\frac{1}{2}x + 4 \quad \textcircled{1}$$

$$y = -\frac{1}{2}x + 4$$

(Total for Question 1 is 4 marks)